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Retrospective GIS-Based Multi-Criteria Decision Analysis: A Case Study of California Waste Transfer Station Siting Decisions

John F. Cirucci, The Pennsylvania State University, Dept. of Geography, johncirucci@gmail.com Douglas A. Miller, The Pennsylvania State University, Dept. of Geography, miller@eesi.psu.edu Justine I. Blanford, The Pennsylvania State University, Dept. of Geography, jib18@psu.edu

Abstract. Geographic information science (GIS) and multicriteria decision analysis (MCDA) disciplines combine to provide valuable insights which guide decision-makers evaluating complex spatial criteria and alternatives, especially when there are conflicting stakeholder values and objectives. Although GIS and MCDA methods have been integrated to support forward-looking decision analyses, there is also advantage to applying these methods *retrospectively* in order to decipher the factors that composed previous spatially-complex decisions. The objective of this study is to demonstrate a methodology which applies "retrospective GIS-based MCDA" to characterize decision-maker value preferences in past siting decisions without a priori knowledge of the decision-making process. As a representative case study, retrospective GIS-based MCDA is performed on municipal solid waste transfer station site decisions in Los Angeles County, California.

Potential attribute data were identified and compiled into a geographic information system. The attributes of actual facility sites and their surrounding vicinities were established as the presence case for a positive decision. This decision problem was structured considering two MCDA decision model types – *value function* using weighted linear combination and *reference point*. The attributes of historical site selections were decomposed and compared to unselected sites to identify attribute patterns. The value function MCDA model was parameterized using logistic regression to establish relative attribute weights which were applied to create a probability spatial distribution profile. The reference point MCDA rule model was parameterized contrasting attribute relative frequency Pareto between transfer station and general locations to create a satisfaction spatial distribution profile. These resulting models provide both relative rank and objective level of attributes represented in previous waste transfer station location decisions. The methodology is applicable to evaluation of spatial decisions in other domains, and can be extended to consider other MCDA decision models.

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Introduction. Every day, we are constantly making simple decisions, considering many criteria. Usually the process is implicit and the decision maker is an individual. In contrast, "multicriteria decision analysis" ("MCDA") describes a collection of formal approaches that can be used to make complex, high impact decisions with multiple stakeholders. The general stages of an MCDA process and two representative decision rule models are depicted in Figure 1. As part of problem structuring, criteria and alternatives are identified. In MCDA, criteria are defined as system attributes or objectives which fulfill a desired outcome. Alternatives are the options from which a final decision is selected. There may be a few alternatives, or an effectively infinite number such as with continuous surface site selection. Problem structuring also requires identification of stakeholders. A significant advantage of many MCDA methods is explicit quantification of stakeholder values. During the model building stage, decision rules are applied to evaluate criteria so the relative worth of possible alternatives can be characterized. Value measurement models entail assigning partial values to all criteria then aggregating these through various combination options to derive a comparative value for each alternative. Reference point models involve establishing a threshold, reference level for each criterion by which alternatives are successively filtered. There are many variants on these and other decision rule types. These two decision rule types were examined in this study. The information that the decision rule model yields is synthesized to establish a course of action (Belton & Stewart, 2002).





b) Two Decision Rule Model Types

Many decisions require spatial consideration – criterion or alternative characteristics may comprise location and proximity. A geographic information system (GIS) can be used in multicriteria decision analysis to assist decision-makers with spatial decisions, and, in fact, GIS-based MCDA is an expanding field with increasing research and application interest. More than 800 peer-reviewed GIS MCDA articles were published between 1990 and 2010 with accelerating frequency covering a broad range of methods, decision problems and application domains (Malczewski & Rinner, 2015). Methodologies for GIS-based MCDA and MCDA, in general, deal entirely with a forward-looking view, resolving a current problem to achieve an improved *future* outcome. Alternatively, there could be significant information derived from *past* decisions that involved conflicting stakeholder objectives and complex evaluation of alternatives.

Hypothesis. Thus, could evidence on historical, third-party decisions be reverse-engineered to elicit information about the stakeholders' values and the decision-making process?

In this study, geospatial statistical analyses were integrated with multiple criteria decision analysis methods to *retrospectively* examine prior location decisions which entailed multiple stakeholders with conflicting motivations and data uncertainty. An inverse problem approach was applied to evaluate possible criteria, develop value preference parameters and test different MCDA decision rule models without explicit information about stakeholders' values or decision processes. The objectives were to (1) create a probabilistic model for prediction of future related decision outcomes; (2) provide insights in decision-maker strategies; and (3) develop and demonstrate a new methodology applicable to other spatial decision domains. The site selection of municipal solid waste transfer stations (WTS) in Los Angeles County, California, was selected as a representative case study.

Investigative Method. A WTS is a facility for solid waste to be temporarily unloaded from collection vehicles and stored for a short duration, so that it can be reloaded onto large load vehicles for transportation to a final disposal facility (Environmental Protection Agency, 2002). Siting a WTS is a classic NIMBY ("not in my backyard") scenario since residents and business owners will not want to be proximate to the site. The decision maker for siting may be a municipality or commercial entity but there are many stakeholders influencing this decision. Transport distance and cost are important siting considerations. However, there are many other criteria which may be evaluated in decision analysis - community concern over noise, odor, and traffic, land use restrictions, population density and growth rate, WTS capacity and technologies. Some important social characteristics such as local population ethnic and racial demographics may not be explicitly incorporated into decision processes but may be implicitly correlated to outcomes, so these must also be considered. Previous studies identified WTS clustering in low income, non-white communities (Environmental Protection Agency, 2000). There are inevitably other site-specific criteria such as local political objectives and site history which are difficult to broadly incorporate into a general, county-wide study. For this study the data collection strategy was to collect readily available, public information across a breadth of categories. These data were selected to encompass EPA WTS best practice guidance as well as some exploratory, implicit criteria including racial demographics and housing characteristics. The effectiveness in these data describing actual results will indicate the extent of deficiencies from missing information and establish a baseline against which future criteria can be evaluated. Since there are a large number of zoning classes and special zoning areas in LA County, zoning was generally considered as agglomerated land use type based on the database created by the Southern California Association of Governments (2015). The study data consist of WTS location coordinates, waste type, capacity, facility land area, landfill disposal site coordinates, the complete county roadway network, land use classification, elevation, population, demographics (racial, ethnic, gender, age), housing characteristics, and income level. The complete list of study criteria is included in the Supplementary Material, Table S1.

Data Preparation. This study focused on WTS operating between 2000 - 2015 applying 2005 land use classification and 2010 Census demographic data. The Solid Waste Information System (SWIS), maintained by the California Department of Resources Recycling and Recovery, served as the primary source of data on WTS and disposal facilities in California (California Department of Resources Recycling and Recovery, 2014). Effective after 1994, the only WTS in California that require full permits are those with greater than 100 tons per day capacity, designated as "Large Volume Transfer Stations." For the purpose of this study, 41 large volume WTS operating in Los Angeles County (contiguous, excluding islands) between 2000 and 2015 were analyzed.

Demographic data and associated TIGER/Line shapefile geographic boundaries were obtained from the U.S. Census Bureau database at the census block level for 2010 and included age, gender, race, ethnicity and household characteristics (family size, ownership type. Income and poverty level were acquired from the U.S. American Community Survey 5-year estimates available at the block group level for Los Angeles County (United States Census Bureau, 2015). Roads were also obtained as TIGER/Line shapefiles from the US Census Bureau. Slope data

were calculated using the 10-foot Digital Elevation Model (DEM) obtained from the Los Angeles Regional Imagery Acquisition Consortium (Los Angeles County, 2015). Land use data for 2009 were obtained from SCAG (Southern California Association of Governments, 2015).

Since transportation costs are important in the optimization of site selection (Environmental Protection Agency, 2002), this was accounted for by calculating travel time from each cell to all disposal locations within the LA County. The travel time to residents was estimated based on the road distance to serve a population of 60,000 people. Road types not suitable for transfer vehicles, such as bike paths were removed; the remaining road types were assigned a relative transportation cost represented as estimated travel time (Table S2 Supplementary).

All data were spatially converted and assigned to 1 hectare area cells. The contiguous LA County land area is over 1 million hectares. These cells were established as the set of possible site alternatives. The median land area of a transfer station is 2.5 acres in LA County which is approximately consistent with this study area cell resolution. Demographic data (e.g. population, housing, income) and land use at an immediate cell location may not be indicative of the vicinity characteristics. Therefore, the data for the surrounding "neighborhood" (within a radius of 0.25 km) was obtained and the mean value was assigned to each center cell. All data were extracted to tabular format for subsequent statistical analyses.

Analysis. Data analyses were performed using ArcGIS 10.2, R version 3.0.2 (R Core Team, 2013) and Microsoft Excel. A preliminary evaluation of the spatial distribution of WTS in LA County was performed in ArcGIS to identify the extent of non-random distribution and clustering. All attribute data were mapped for visual examination and qualitative pattern identification. Tabular attribute data was examined as boxplots, histograms and density plots. Side-by-side comparison was made for WTS locations versus general locations considering general statistical characteristics – range, mean, median, skew, standard deviation. Mean difference and Chi-squared test probabilities were computed. Two general MCDA decision rule models were evaluated using this dataset: *Value Function* type and *Reference Point* type.

Value Function Decision Model. For the value function model form, a simple weighted linear combination was considered. Data were regressed to establish attribute weights which provide a sum of products value for any given location alternative. Higher values should correspond to more preferred locations. The dependent variable is the presence indication of a transfer station at a given location, represented as 1 or 0, for present or not present, respectively. Since this outcome is binary, a logistic regression was performed. Attributes were fitted to the model form:

 $y_{transfer} = 1 / [1 + exp^{-}(c_0 + c_1x_1 + c_2x_2 + ...)]$

Where, y_{transfer} = probability of the WTS presence,

 c_0 = intercept, c_i = attribute *i* weight x_i = attribute *i* value.

Logistic regression model goodness-of-fit was evaluated considering changes in residual deviance versus null deviance. Relative comparisons of model forms were performed using deviances (log likelihood ratios) and Akaike information criteria (AIC). Attribute significance and collinearity were evaluated considering P-value, variance inflation factor (VIF) and condition indices (Hosmer, Lemeshow, & Sturdivant, 2013). AIC represents a trade-off between model fit and collinearity, and was used as the final optimization parameter. Individual attributes were iteratively removed based on lowest rank confidence of statistical mean difference between WTS and general locations, evidence of collinearity, and stepwise improvement in fit. Attribute

combinations were evaluated and removed iteratively to progressively improve model fit and reduce multicollinearity. Linear combination of the sum product of weights and attribute values provide the logit value which was then transformed into a WTS logistic probability assigned to each cell. This table of probabilities retaining its spatial georeferences was imported back into ArcGIS to produce a WTS probability distribution map for LA County.

Reference Point Decision Model. The reference point decision rule model required the identification of significant maximum or minimum attribute thresholds. These were fitted by comparison of the attribute ranges and distribution profiles of actual WTS locations versus general locations. For each attribute, relative frequency (frequency/total) Pareto plots of WTS locations and general locations were created using the 41 WTS attribute values as bin increments. From these, the WTS:general relative frequency ratio was computed as a function of attribute value. Ratios greater than one imply that an attribute has a negative impact – that is, the frequency is increasing faster for WTS locations than for general locations over an attribute's range. The opposite holds true for relative frequency ratios less than one. These are consistent with the mean difference analyses. Potential attribute reference points are indicated when there is a discontinuity or change in slope toward unity for these ratios. The reference point is a maximum threshold for ratios > 1 and a minimum threshold for ratios < 1. Reference points are not necessarily indicated for all attributes and some threshold indications were indistinct. For this study, obvious reference points were classified as "tier 1." Weak reference points - defined as those which occurred when WTS relative frequency was less than 50% or when there was variability in the slope change - were classified as "tier 2." These reference points were applied to classify attributes for all cells in the full dataset. In ArcGIS the individual attribute raster layers were reclassified from a value range to a binary indication of a reference point satisfaction (1= satisfied, 0=not satisfied). These individual attribute, binary raster layers were then processed to three different spatial distributions:

- Product of all tier 1 binary reference point raster layers
- Product of all tier 1 and 2 binary reference point raster layers
- Sum of all tier 1 and 2 binary reference point raster layers

The two product combinations represent a conventional reference point decision rule resulting in a binary outcome for WTS satisfaction. The combined tier 1 and 2 rasters is most restrictive. The sum combination is a non-conventional reference point decision rule but provides a satisfaction gradient.

The value measurement probability results and reference point satisfaction results were mapped across LA County to provide a visualization of their distributions and comparative responses.

Results. Spatial distribution analysis of the active "large volume" WTS revealed a non-random distribution within LA County with an average mean distance of 3.1 km between stations versus a random distributed distance of 4.6 km. A low p-value (0.000084) and large negative z-score (-3.933) indicated low probability of random distribution and an observed mean distance between stations at about 2 standard deviations below a random distribution level. This was expected since WTS were seen to be clustered in proximity to the higher population density areas. Statistical comparison of attributes for WTS locations versus general locations indicate >95% confidence of significant mean difference for 19 of the 27 attributes (Supplemental Information Table S3).

The retrospective value measurement logistic regression initially fit all attributes (27) as a baseline giving expectedly poor fit. Following 17 model improvement iterations, the final form

was resolved comprising 11 attributes with significant, non-collinear model contribution. The value measurement probability distribution and normalized attribute weights are shown in Figure 2. Transportation times which directly impact WTS operating economics dominate the model fit. However, 6 demographic/social attributes significantly and independently impact WTS probability. This does not directly implicate causality in the decision process but these attributes are not collinear with other study attributes. The absolute value preference probabilities are quite low, less than 0.02. This is expected since there is a small, discrete number of WTS required across the county yielding a randomly distributed probability of only 0.00004.



Figure 2. Normalized Attribute Weights and Value Measurement Probability Distribution

Retrospective reference point evaluation yielded 7 "tier 1" attributes and 4 "tier 2" attributes. 8 of these attributes were consistent with the value measurement results. The resulting satisfaction distributions for the three alternate reference point treatments are shown in Figure 3. Tier 1 and tier 1&2 products satisfied only 52% and 39% of actual WTS locations, respectively. However, these satisfaction frequencies were much higher than general locations, at 9% and 3%.



a) Tier 1 Product Layer b) Tier 1 & 2 Product Layer c) Tier 1 & 2 Sum Layer Figure 3. Reference Point Satisfaction Distribution for Los Angeles County WTS

Discussion. Retrospective value measurement analysis provided a well-fit probabilistic model predicting greater than 40 times mean higher probability for actual WTS site locations, and confirming the significance of transportation economic contribution while also indicating social demographic bias in decision outcomes. Retrospective reference point satisfaction was a

simpler, non-regression method. Since the product aggregation of reference points is a restrictive filtration, the proportion of satisfactory sites becomes small as the number of attributes increases, so this approach might be best suited for decisions with a limited number of well-defined attributes. Both methods yielded practical and reasonably consistent results. In addition to further enhancement on these retrospective methods, useful future research should explore other MCDA methods such as outranking and the analytical hierarchy process.

Retrospective GIS-based MCDA can be applied to improve future decision analyses by providing explicit information about related past decisions, perhaps even revealing unintended and undesirable criteria correlation. It may also serve as an investigative tool to reveal external party strategies in commercial competitive analyses or military intelligence.

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Supplementary Information

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John F. Cirucci The Pennsylvania State University, johncirucci@gmail.com Douglas A. Miller The Pennsylvania State University, miller@eesi.psu.edu Justine I. Blanford The Pennsylvania State University, jib18@psu.edu

Attributes

The attribute criteria for which decision rules were evaluated are listed in Table S1.

Table ST. Final Attribute Data Evaluated in Decision Rule Models										
Field Name	Description	Туре	Category							
OBJECTID	feature identification	ordinal	identifier							
Transfer2015	transfer station present (1,0)	ordinal	classifier							
Disposal2010	disposal facility present (1,0)	ordinal	classifier							
LandUse05	SCAG land use aggregate code at location	nominal	classifier							
TimeDispNr	Time Distance to nearest disposal facility	ratio	attribute - distance							
TimeDispMn	Mean Time Distance to all disposal facility	ratio	attribute - distance							
TimePop60k250	Time (Cost Distance) to nearest 60000 population	ratio	attribute - distance							
PopDens250	Population near (population per km2)	ratio	attribute - demographic							
PopFrWh250	Population fraction White at radius near	ratio	attribute - demographic							
PopFrBl250	Population fraction Black at radius near	ratio	attribute - demographic							
PopFrAs250	Population fraction Asian at radius near	ratio	attribute - demographic							
PopFrHi250	Population fraction Hispanic/Latino origin near	ratio	attribute - demographic							
PopFrFem250	Population over 20 years old fraction female near	ratio	attribute - demographic							
MednAge250	Median age near	ratio	attribute - demographic							
HousDens250	Housing units near (housing units per km2)	ratio	attribute - housing							
HousFrVac250	Housing units fraction vacant near	ratio	attribute - housing							
HousFrRnt250	Housing units occupied fraction rented near	ratio	attribute - housing							
HousAvgSz250	Average household size of occupied housing units near	ratio	attribute - housing							
Slope	Percent slope	ratio	attribute - terrain							
LU05COM250	Fraction commercial land use near	ratio	attribute - land use							
LU05PUB250	Fraction public land use near	ratio	attribute - land use							
LU05MIL250	Fraction military land use near	ratio	attribute - land use							
LU05IND250	Fraction industrial land use near	ratio	attribute - land use							
LU05TRN250	Fraction transportation and utility land use near	ratio	attribute - land use							
LU05REC250	Fraction recreational land use near	ratio	attribute - land use							
LU05AGR250	Fraction agricultural land use near	ratio	attribute - land use							
LU05WAT250	Fraction water land use near	ratio	attribute - land use							
LU05VAC250	Fraction vacant land use near	ratio	attribute - land use							
LU05RES250	Fraction residential land use near	ratio	attribute - land use							
PovertyFrac250	Fraction individuals below poverty level near	ratio	attribute - affluence							
IncomePerCap250	Income per capita near	ratio	attribute - affluence							

Table S1. Final Attribute Data Evaluated in Decision Rule Models

Travel Time Estimation

Road data acquired as MAF/TIGER shapefiles included class codes. These were aggregated and assigned cost factors as shown in Table S2. A nominal speed limit was applied to these road types. An integer value cost factor was set, inversely proportional to the nominal road speed. Travel time was approximated from the cost factor as given in Equation S1.

 $t_{travel}, h = \frac{d_{road \ cost}, cell}{3 \ cost \ factor \times 60^{\frac{mi}{h}} \times 1.61^{\frac{km}{mi}} \times 10^{\frac{cell}{km}}} = \frac{d_{road \ cost}, cell}{2900 \ cell/h}$ (Equation S1)

Allocation to each waste transfer station was made on the basis of population, not land area. Municipal solid waste generation per capita has been relatively flat since 1990 but recycle and compost recovery has been increasing so that net disposal has fallen from 1.7 to 1.3 kg per

person from 1990 to 2012 (Environmental Protection Agency, 2014). On the basis of 1.5 kg per person, a California "large volume" transfer station operating at the minimum permit capacity of 100 tons per day would serve about 60,000 residents. This was used as the reference population level for any potential transfer station location to determine an impact radius as Euclidean distance and travel time based on road network. For consideration of the transportation time between population locations and potential WTS locations, both population density and transportation cost factor were taken together. A representative criteria, t_{60kPop} was established to serve as a surrogate value for transportation time to serve 60,000 individuals as given in Equation S2. This was first established for each cell then averaged for the surrounding neighborhood within a radius of 0.25 km.

$$t_{60kPop}, h = \left(\frac{d_{road \ cost}, cell}{2900 \ cell/h}\right) \times \left(\frac{60000 \ individuals}{\rho_{population}, cell^{-1}}\right)$$
(Equation S2)

MTFCC	Feature Class	Nominal Speed Limit	Cost Factor
S1100	Primary Road	60	3
S1200	Secondary Road	45	4
S1400	Local Neighborhood Road, Rural Road, City Street	15	12
S1500	Vehicular Trail (4WD)		
S1630	Ramp		
S1640	Service Drive usually along a limited access highway	5	36
S1730	Alley		
S1740	Private Road for service vehicles		
Null	No road		360

Table S2. Relative Roadway Cost Factors Based on MAF/TIGER Feature Class Codes

Preliminary Summary Statistics

Summary statistics for attribute data including comparison of WTS and general locations is shown in Table S3. The mean difference Z-score was calculated per equation S3. This is a dimensionless difference between WTS and general attribute values normalized based on their standard deviations. An associated p-value represents the probability that there is no significant mean difference (null hypothesis). Hence a p-value less than 0.05 indicates a 95% confidence the difference of the means is significant. However, most of these attribute data were not normally distributed causing skew in the Z-score. Therefore, a Chi-squared p-value was also determined. The Chi-square test was applied to attribute frequency divided into bins corresponding to the general data quartile breaks.

$$Z_{\Delta mean} = \frac{(\mu_{wts} - \mu_{all})}{\sqrt{\frac{\sigma_{wts}^2}{N_{wts}} + \frac{\sigma_{all}^2}{N_{all}}}}$$
(Equation S3)

Where

wts = waste transfer station location attribute all = general location attribute μ = attribute mean σ = standard deviation

N = count

There were 21 attributes that presented 95% confidence for significant mean difference between WTS and general locations.

	Transfer St	ation Locat	ions (n=41)	All Loc	ations (n=1	027377)	7-score	D value	D-value	
Attribute	Mean	Median	Standard Deviation	Mean	Median	Standard Deviation	∆mean/SD	Z-score	χ2 Test	
TimeDispNr	98	93	26	464	168	732	-89.4	0.0000	0.0000	
TimeDispMn	237	229	26	608	315	727	-89.7	0.0000	0.0000	
TimePop60k250	39060	3611	109006	7357330	60045	23278749	-221.0	0.0000	0.0000	
PopDens250	776	286	1152	950	2	2161	-1.0	0.2495	0.0035	
PopFrWh250	0.54	0.56	0.26	0.67	0.72	0.27	-3.1	0.0028	0.0117	
PopFrBl250	0.09	0.02	0.15	0.06	0.01	0.15	0.9	0.2734	0.3422	
PopFrAs250	0.09	0.04	0.18	0.09	0.02	0.16	0.0	0.3989	0.4174	
PopFrHi250	0.55	0.64	0.37	0.28	0.17	0.28	4.3	0.0000	0.0000	
PopFrFem250	0.45	0.50	0.16	0.48	0.50	0.14	-1.0	0.2538	0.1772	
MednAge250	35.6	31.8	8.9	43.1	43.5	11.9	-4.9	0.0000	0.0003	
HousDens250	258	79	459	333	1	811	-1.0	0.2320	0.0058	
HousFrVac250	0.05	0.03	0.10	0.15	0.05	0.23	-5.7	0.0000	0.0210	
HousFrRnt250	0.61	0.53	0.30	0.32	0.21	0.31	5.5	0.0000	0.0000	
HousAvgSz250	3.39	3.33	1.41	2.78	2.75	1.09	2.4	0.0222	0.0094	
Slope	1.6	0.9	2.4	15.3	7.2	17.9	-37.3	0.0000	0.0000	
LU05COM250	0.04	0.00	0.09	0.02	0.00	0.10	1.0	0.2449	0.0087	
LU05PUB250	0.01	0.00	0.03	0.02	0.00	0.08	-1.7	0.1015	0.6080	
LU05MIL250	0.00	0.00	0.00	0.02	0.00	0.13	-145.7	0.0000	0.8152	
LU05IND250	0.65	0.69	0.28	0.03	0.00	0.14	14.1	0.0000	0.0000	
LU05TRN250	0.17	0.08	0.20	0.03	0.00	0.12	4.7	0.0000	0.0000	
LU05REC250	0.00	0.00	0.00	0.01	0.00	0.07	-128.1	0.0000	0.7775	
LU05AGR250	0.01	0.00	0.05	0.03	0.00	0.16	-2.4	0.0199	0.3920	
LU05WAT250	0.00	0.00	0.00	0.01	0.00	0.08	-113.0	0.0000	0.8623	
LU05VAC250	0.02	0.00	0.05	0.61	0.92	0.45	-73.2	0.0000	0.0000	
LU05RES250	0.08	0.00	0.18	0.19	0.00	0.33	-4.1	0.0001	0.0056	
PovertyFrac250	0.22	0.22	0.12	0.12	0.09	0.11	4.9	0.0000	0.0000	
IncomePerCap2 50	22737	19234	10950	34275	30246	19080	-6.7	0.0000	0.0008	

Null hypothesis probability > 5%

Attribute data were also examined visually through boxplots and histograms. Four representative histograms generated in R are shown in Figure S1.





Value Measurement Decision Rule

The logistic regression performed to determine value measurement attribute coefficients proceeded through 17 iterations with the goal to attain goodness of fit while minimizing multicollinearity between attributes. The progression of these iterations is summarized in Table S4.

The final iteration resulted in coefficients that were then applied in the logistic form to derive a WTS probability for each cell in the study area. A small scale map of this probability distribution covering the City of Los Angeles is depicted in Figure S2 showing good correspondence with all current WTS locations.

Table S4. Value Measurement Logistic Regression Iteration Log

RUN	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
Dresid	912.6	486.7	490.9	493.2	516.4	516.5	490.6	503.4	490.7	490.7	490.7	490.7	490.8	490.9	490.8	490.9	518.3	491.2
Dnull	912.6	684.4	684.4	684.5	684.5	684.5	684.4	684.4	684.4	684.4	684.4	684.4	684.4	684.4	684.4	684.4	724.9	684.4
R2L	0.000	0.289	0.283	0.279	0.246	0.245	0.283	0.264	0.283	0.283	0.283	0.283	0.283	0.283	0.283	0.283	0.285	0.282
AIC	914.57	542.70	530.90	527.20	542.40	540.50	530.58	539.37	528.65	526.66	524.70	522.73	520.77	520.87	518.79	516.89	542.34	515.18
Paic	0.0000	0.0000	0.0004	0.0025	0.0000	0.0000	0.0005	0.0000	0.0012	0.0032	0.0086	0.0229	0.0611	0.0581	0.1645	0.4253	0.0000	1.0000
signif var	0	0	2	2	1	1	2	2	2	2	2	2	2	2	2	2	2	2
VIF>7.5	0	5	5	2	0	0	3	0	1	0	0	0	0	0	0	0	0	0
COEFFICIENTS																		
Intercept	-10.13	-11.01	-8.87	-9.81	-8.28	-8.40	-10.75	-6.62	-10.70	-10.56	-10.64	-10.82	-10.86	-10.96	-10.82	-10.91	-9.68	-11.27
TimeDispNr	0.00E+00	1.29E-02	9.95E-03	0.00E+00	-7.78E-03	0.00E+00												
TimeDispMn	0.00E+00	-1.86E-02	-1.48E-02	-5.96E-03	-1.74E-06	-7.90E-03	-5.73E-03	-7.91E-03	-5.72E-03	-5.75E-03	-5.89E-03	-5.95E-03	-5.96E-03	-5.95E-03	-6.00E-03	-5.98E-03	-6.61E-03	-5.64E-03
TimePop60k250	0.00E+00	-1.69E-06	-1.47E-06	-1.54E-06	0.00E+00	-1.70E-06	-1.45E-06	-1.62E-06	-1.47E-06	-1.47E-06	-1.49E-06	-1.48E-06	-1.47E-06	-1.45E-06	-1.47E-06	-1.45E-06	-1.32E-06	-1.39E-06
PopDens250	0.00E+00	-1.54E-04	-1.64E-04	0.00E+00	0.00E+00	0.00E+00	-1.61E-04	-1.53E-04	-8.67E-05	-8.17E-05	-7.04E-05	-6.96E-05	-6.95E-05	-7.20E-05	-7.09E-05	-7.40E-05	-6.52E-05	0.00E+00
PopFrWh250		-0.096	0.006	-0.080	-0.301	-0.263								0.035				
PopFrBI250		-0.463					-0.353	-0.309	-0.367	-0.370	-0.364	-0.363	-0.380		-0.377			
PopFrAs250		0.0470																
PopFrHi250		0.413	0.548	0.579	0.896	0.814	0.412	0.577	0.383	0.383	0.390	0.354	0.361	0.459	0.359	0.462	0.134	0.450
PopFrFem250		1.12					1.05	0.81	1.04	1.04	1.05	1.06	1.10	1.11	1.11	1.11	0.23	1.11
MednAge250		-0.0194	-0.0206	-0.0180			-0.0194	-0.0186	-0.0195	-0.0194	-0.0193	-0.0172	-0.0172	-0.0171	-0.0172	-0.0168	-0.0270	-0.0161
HousDens250	0.00E+00	2.49E-04	2.26E-04	-7.30E-05	-7.54E-04	-7.49E-04	2.19E-04	0.00E+00										
HousFrVac250		-0.586	-0.841	-0.475	-0.379	-0.275	-0.533	-0.616	-0.471	-0.478	-0.520	-0.432						
HousFrRnt250		0.243	0.149	0.343	0.942	0.952	0.273	0.365	0.288	0.281	0.273	0.294	0.301	0.307	0.312	0.318		0.275
HousAvgSz250		-0.0416	-0.0377	-0.0413	-0.0419		-0.0258	-0.0518	-0.0345	-0.0339	-0.0334							
Slope		-0.0575	-0.0596	-0.0631	-0.0822	-0.0822	-0.0605	-0.0521	-0.0607	-0.0606	-0.0641	-0.0638	-0.0636	-0.0624	-0.0645	-0.0631	-0.0674	-0.0599
LU05COM250		2.750	0.372	0.151	-1.429	-1.388	0.267	-3.263	0.297	0.141	0.246	0.272	0.267	0.256				
LU05PUB250		1.28																
LU05MIL250		-150																
LU05IND250		8.01	5.71	5.81	3.92	3.94	5.78	2.38	5.77	5.64	5.74	5.75	5.76	5.73	5.72	5.69	5.80	5.97
LU05TRN250		7.65	5.29	5.39			5.44		5.43	5.29	5.40	5.42	5.42	5.40	5.38	5.36	5.64	5.65
LU05REC250		-158																
LU05AGR250		5.26																
LU05WAT250		-160																
LU05VAC250		2.060	-0.208	-0.144			-0.253	-3.714	-0.275	-0.416								
LU05RES250		2.469	0.254	-0.043			0.236	-3.149	0.207									
PovertyFrac250		2.06	2.01				2.34	2.02	2.31	2.31	2.28	2.28	2.25	2.18	2.24	2.17	2.21	2.03
IncomePerCap250	0.00E+00	1.18E-05	1.18E-05	7.96E-06	1.33E-06	1.33E-06	1.15E-05	8.49E-06	1.18E-05	1.19E-05	1.22E-05	1.22E-05	1.21E-05	1.23E-05	1.20E-05	1.23E-05	1.03E-05	1.28E-05



Figure S2. Value Measurement WTS Probability Distribution, City of Los Angeles

Reference Point Decision Rule

The relative frequency ratio analysis described in the main paper is represented graphically for two attributes in Figures S3 and S4. In Figure S3 the ratio for vacant housing fraction indicates a distinct slope change at an attribute level of 0.06. This was interpreted as a reference point maximum threshold.



Figure S3. Relative Frequency Ratio WTS: General Location for Vacant Housing Fraction

In Figure S4 the ratio for industrial land use fraction is shown. Although there is a significant mean difference between WTS and general locations, there is no distinct discontinuity in the ratio, hence no reference point threshold was identified.



Figure S4. Relative Frequency Ratio WTS: General Location for Industrial Land Use Fraction

The reference point values were applied to the study area and each cell classified according to three different reference point aggregation forms. The frequency of satisfactory designations for WTS and general locations is shown Figure S5.



Figure S5. Reference Point Satisfaction Frequency – WTS vs. General Location Comparison

The reference point satisfaction distribution for the City of Los Angeles is depicted in Figures S6, S7 and S8 for the tier 1 product, tier 1&2 product and tier 1&2 sum aggregation methods, respectively.



Figure S6. Reference Point Tier 1 Product Satisfaction Distribution, City of Los Angeles



Figure S7. Reference Point Tier 1 & 2 Product Satisfaction Distribution, City of Los Angeles



Figure S8. Reference Point Tier 1 & 2 Sum Satisfaction Distribution, City of Los Angeles